

EVF 2011: 1. sem

03/04/2018

QL
a)



$$x = \phi R$$

$$\dot{x} = \dot{\phi} R$$

first looking rotation
• displacement of the CM

$$\hat{\gamma} = I \alpha$$

$$F_f \cdot R = (I + mR^2) \frac{a}{R}$$

b) $m\ddot{x} = F_x - F_{ct} \Rightarrow m\ddot{x} = mg \sin \theta - mg \cos \theta \cdot \mu$

$$\ddot{x} = g \sin \theta - g \cos \theta \cdot \mu$$

$$\Rightarrow a = g \sin \theta - (I + mR^2) \frac{a}{R^2}$$

$$\ddot{x} = \frac{g \sin \theta}{[1 + \frac{I}{mR^2}]}$$

c) $mgh = \frac{mv^2}{2} + \frac{I\omega^2}{2}$ (if for wheels)
 \hookrightarrow principle of conservation of energy

Q3.

a) $U_r = \frac{mv^2}{r} \Rightarrow mvn^2 = \frac{h^2}{h} \Rightarrow \sqrt{\frac{h^2 n^2}{m}} = \frac{\sqrt{h^2 n^2}}{\sqrt{m}} = v_n, n > 0$

b) $E = \frac{p^2}{2m} + \frac{q^2 r^2}{2} = \frac{mv^2}{2} + \frac{q^2 r^2}{2} = \frac{mv^2}{2} \Rightarrow E = \frac{v \cdot nh}{\sqrt{m}} = \sqrt{\frac{v}{m}} \cdot nh$

$$mv^2 = nh^2/r^2$$

$$\Delta E = E_2 - E_1 = h \sqrt{\frac{v}{m}} \Rightarrow E = h \sqrt{\frac{v}{m}} \Rightarrow v = \sqrt{\frac{v}{m}}$$

c) $p = \frac{h}{\lambda} \quad E_2 = 2h \sqrt{\frac{v}{m}}$

$$E = \frac{p^2}{2m} = \frac{h^2}{2m\lambda^2} \Rightarrow \lambda = \frac{h}{\sqrt{2Em}}$$

$$\lambda = \sqrt{\frac{h^2 n}{2mK}} = \sqrt{\frac{m h^2}{K}}$$

□

$$d) n\lambda = z d \sin \theta$$

$$n\lambda_1 = 2.018 \cdot 10^{-6} \dots$$

Q4.

$$a) K_{\text{max}} = h\nu_0 - \phi = 0.5 \text{ eV} \quad E = \frac{hc}{\lambda} = \frac{9.11 \cdot 10^{-31} \cdot 3 \cdot 10^8}{9.19 \cdot 10^{-8}} = 3.0 \text{ eV}$$

b) note, a photon can be absorbed by a free electron.

$$c) \lambda' - \lambda = \frac{h}{m_0 c} (1 - \cos \theta) \quad \begin{array}{l} \lambda, \nu, E \\ \lambda', \nu', E' \\ \searrow K, p \end{array} \quad E' = \frac{E}{2}$$

$$\lambda' = \lambda_c (1 - \cos \theta) + 2\lambda_c = \lambda_c (3 - \cos \theta) \quad E = E' + K$$

$$\frac{E}{2} = K \Rightarrow E = 2K$$

$$\lambda' = \frac{hc}{E'} = \frac{2hc}{E} = \frac{2hc}{2K} = \frac{hc}{K} = \frac{hc}{\lambda_c}$$

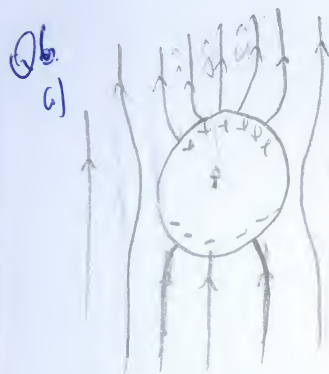
$$\Rightarrow \frac{hc}{\lambda_c} = 3 - \cos \theta \Rightarrow \theta = \cos^{-1} \left(3 - \frac{hc}{\lambda_c} \right)$$

$$d) K = \frac{E}{2} = \frac{m_0 c^2}{2} \quad p = \frac{m_0 c}{2} \dots$$

$$p^2 = K^2 + 2Km_0 \Rightarrow \frac{m_0^2 c^2}{2} + m_0^2 c^2 = p^2 = \frac{3m_0^2 c^2}{2} = m_0 c \sqrt{\frac{3}{2}}$$

EVF 2011-25m

0369



eletrostático equilíbrio. As cargas vão se rearranjar
que o campo elétrico fique perpendicular à superfície
Cargas na superfície do interior e ele tem as cargas
reguladas e casca no ponto. Então o campo
o campo é nulo. As cargas tendem a deixar o corpo

b) $E = E_0 \hat{z}$

$V = -E_0 z + C$



d)



Q8. a) $\int_{-\infty}^{\infty} A^2 e^{-\frac{2\mu\omega}{\hbar} x^2} dx = 1$

$A = \sqrt{\frac{\mu\omega}{\pi\hbar}} ; B = \sqrt{\frac{9\mu\omega^3}{\pi\hbar}}$

b) para ψ_0 na eq. de $E_0 = \frac{\hbar\omega}{2}$

c) $\langle x \rangle = \int_{-\infty}^{\infty} \psi^* x \psi dx$ temo no nulo sua função exponencial $= \int_{-\infty}^{\infty} x e^{-x^2} dx = 0$

$\frac{d\langle x \rangle}{d\beta} = 0 ; \frac{d^2\langle x \rangle}{d\beta^2} \text{ (probabilidade)}$

d) $\psi(x,t) = e^{-\frac{i\hbar\omega}{2}} \psi_0 + e^{-\frac{i\hbar\omega}{2}} \psi_1 ; \psi(x,t) = \int \psi(x,t) \psi(x,t) dx$

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Q9. c)

$$L_{\pm} = L_x \pm iL_y \Rightarrow \boxed{L_x = \frac{L_+ + L_-}{2}}$$

$$L_- = L_x - iL_y$$

$$L_{\pm} Y_{lm} = \hbar \sqrt{l(l+1) - m(m \pm 1)} Y_{l, m \pm 1}$$

$$l=1 \Rightarrow m = -1, 0, 1$$

$$L_+ |1, -1\rangle = \sqrt{2}\hbar |1, 0\rangle$$

$$L_+ |1, 0\rangle = \sqrt{2}\hbar |1, 1\rangle \Rightarrow L_x \begin{bmatrix} \langle 1, -1 | L_+ | 1, -1 \rangle & \langle 1, 0 | L_+ | 1, -1 \rangle & \langle 1, 1 | L_+ | 1, -1 \rangle \\ \dots & \dots & \dots \end{bmatrix}$$

$$L_- |1, 1\rangle = 0 |1, 2\rangle$$

$$L_x = \begin{bmatrix} 0 & \sqrt{2}\hbar & 0 \\ 0 & 0 & \sqrt{2}\hbar \\ 0 & 0 & 0 \end{bmatrix} \quad L_z = \begin{bmatrix} 0 & 0 & 0 \\ \sqrt{2}\hbar & 0 & 0 \\ 0 & \sqrt{2}\hbar & 0 \end{bmatrix}$$

$$L_- |1, -1\rangle = 0 |1, -2\rangle$$

$$L_- |1, 0\rangle = \sqrt{2}\hbar |1, -1\rangle$$

$$L_- |1, 1\rangle = \sqrt{2}\hbar |1, 0\rangle$$

$$\boxed{L_x = \frac{L_+ + L_-}{2} = \frac{\sqrt{2}\hbar}{2} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}}$$

$$b) \begin{vmatrix} -\lambda & \frac{\hbar}{\sqrt{2}} & 0 \\ \frac{\hbar}{\sqrt{2}} & -\lambda & \frac{\hbar}{\sqrt{2}} \\ 0 & \frac{\hbar}{\sqrt{2}} & -\lambda \end{vmatrix} = 0 \Rightarrow -\lambda^3 + \hbar^2 \lambda = 0 \Rightarrow \lambda(-\lambda^2 + \hbar^2) = 0$$

$$\boxed{\lambda = 0, \lambda = \pm \hbar}$$

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c) $\lambda = t$

$$\frac{t}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} a \\ b \\ c \end{bmatrix} = t \begin{bmatrix} a \\ b \\ c \end{bmatrix} \Rightarrow \frac{b}{\sqrt{2}} = a$$

$$\frac{a+c}{\sqrt{2}} = b \Rightarrow c = a$$

$$\left[\frac{b}{\sqrt{2}} \quad b - \frac{b}{\sqrt{2}} \right] \begin{bmatrix} \frac{b}{\sqrt{2}} \\ b \\ \frac{b}{\sqrt{2}} \end{bmatrix} = 1$$

$$= 2b^2 = 1 \Rightarrow b = \frac{1}{\sqrt{2}} \Rightarrow \begin{bmatrix} \frac{1}{2} \\ \frac{1}{\sqrt{2}} \\ \frac{1}{2} \end{bmatrix}$$

$$\begin{bmatrix} \frac{b}{\sqrt{2}} \\ b \\ \frac{b}{\sqrt{2}} \end{bmatrix}$$

d) $L_2 = \begin{bmatrix} h & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & h \end{bmatrix} \Rightarrow L_2 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \Rightarrow \langle L_2 | L_1 \rangle = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} \frac{1}{2} \\ \frac{1}{\sqrt{2}} \\ \frac{1}{2} \end{bmatrix}$

$$ah = ah$$

$$-hc = hc$$

$$P(L_2) = \frac{1}{4}$$

$$\lambda = 0 \quad L_2 \begin{bmatrix} h & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & -h \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = 0 \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

$$\begin{matrix} ah = 0 \\ -hc = 0 \\ 0 = 0 \end{matrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \frac{1}{2} \\ \frac{1}{\sqrt{2}} \\ \frac{1}{2} \end{bmatrix} \Rightarrow P(L_0) = \frac{1}{2}$$

$$\lambda = -h \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \Rightarrow P = \frac{1}{4}$$

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Q10.

$$a) w_2 \int_A^B p dv = \int_V^{2V} \frac{nRT}{V} dv = \underline{nRT \ln 2}$$

$$b) du = dq - dw \quad dT = 0 \text{ porque está trabalhando em volume e a temperatura.}$$

$$du = 0 \quad dv = 0 \quad dw = 0$$

$$dq = dw \Rightarrow \boxed{Q = nRT \ln(2)}$$

$$c) \theta = T \Delta S$$

$$\boxed{\Delta S_g = nR \ln 2} \text{ pl gases}$$

$$d) \Delta U > 0$$

$$\Delta w > 0 \text{ (exp. livre)}$$

$$\Delta \theta = 0$$

$$du = 0$$

$$\begin{aligned} S_g &= nR \ln 2 \\ S_u &= 0 \end{aligned} \quad \boxed{\Delta S_T = nR \ln 2}$$

$$\theta_g + \theta_r = 0 \text{ reversível}$$

$$\theta_g = -\theta_r \Rightarrow \boxed{\Delta S_r = -nR \ln 2}$$

$$\Delta S_T = 0 \text{ (processo reversível)}$$